



The von Karman Institute  
for Fluid Dynamics



# On The Dynamic Response of Constant Temperature Hot-Wire Anemometers (CTHWA)

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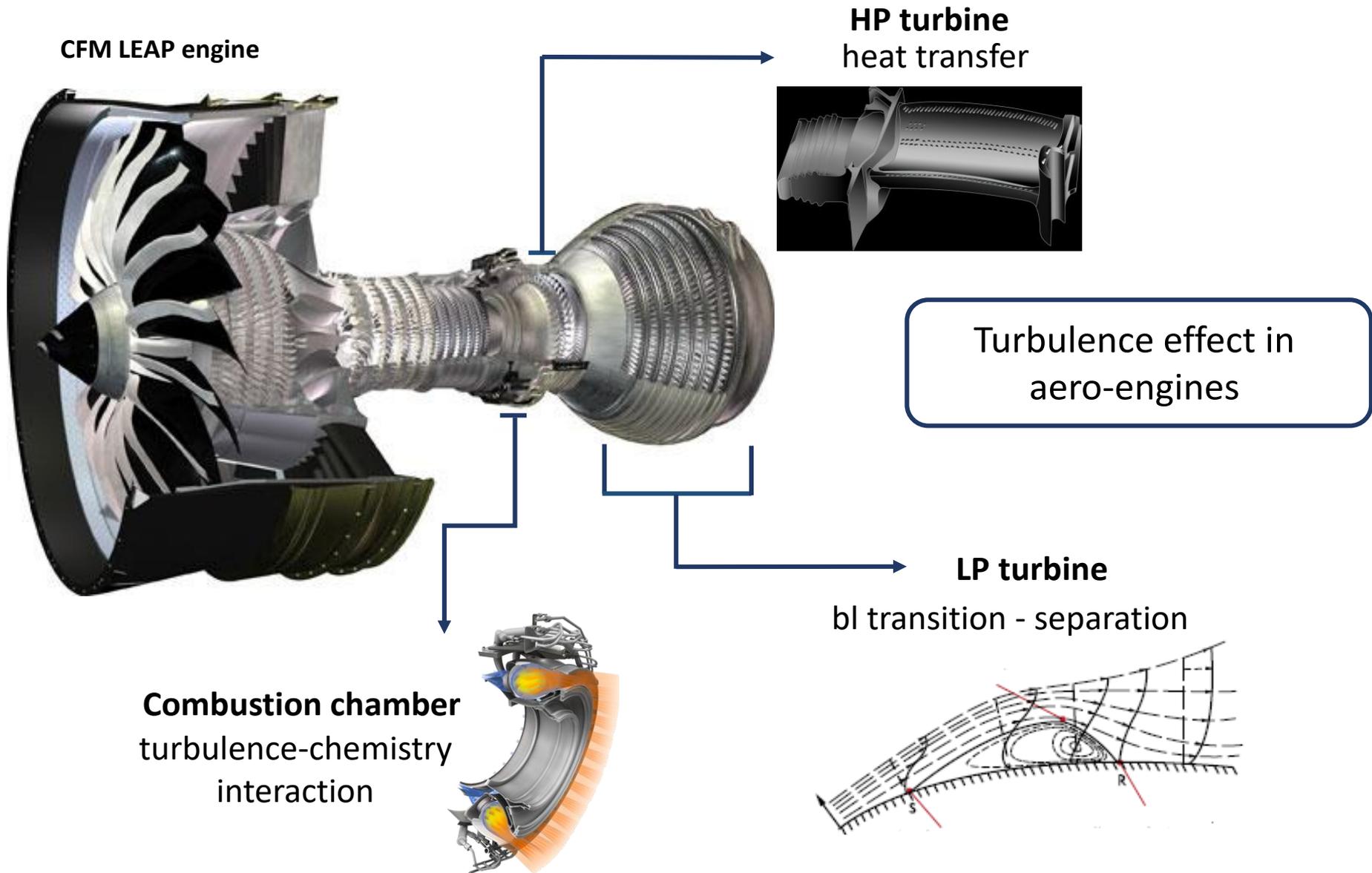
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University supervisor: Tony Arts (UCL/VKI)

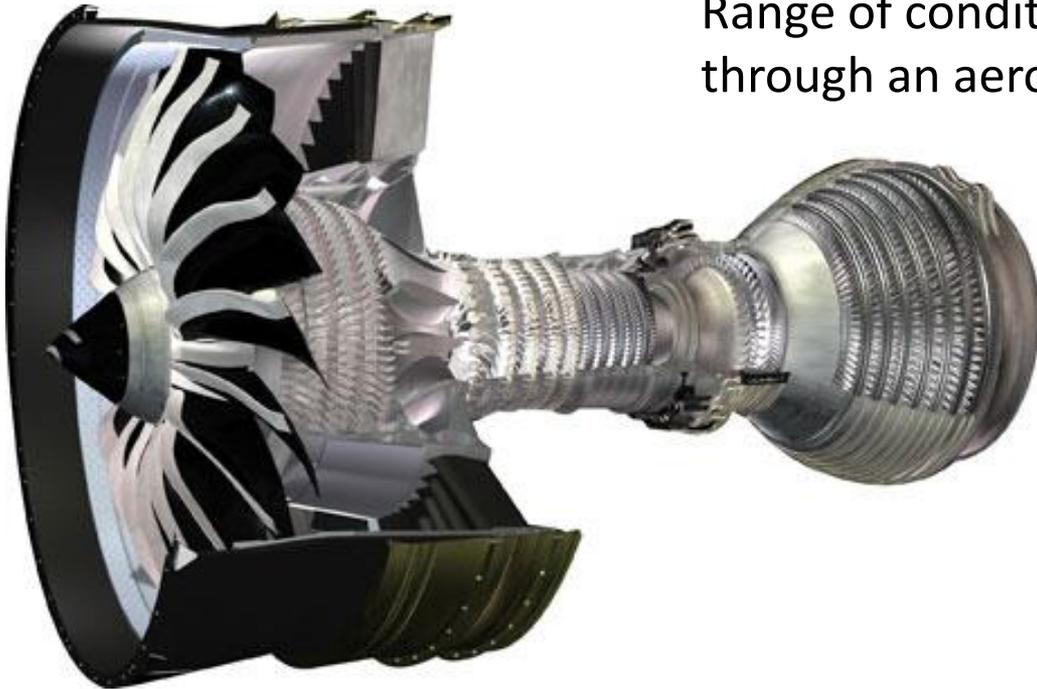


# Context



# Context

CFM LEAP engine



Range of conditions  
through an aero-engine:

**$M$** : 0.1~1.2

**$BPF$** : 1~15 kHz

**$Tu$** : > 10% ?



*High speed flow*  
*Unsteady phenomena*  
*High turbulence level*



Turbulence measurements  
in turbomachinery flows:

***High frequency response***  
***High spatial resolution***

# Why CTHWA?

## Constant Temperature Hot-Wire Anemometry (CTHWA)

High spatial resolution:

$$d_{wire} \sim 5 - 10 \mu m$$

High frequency response:

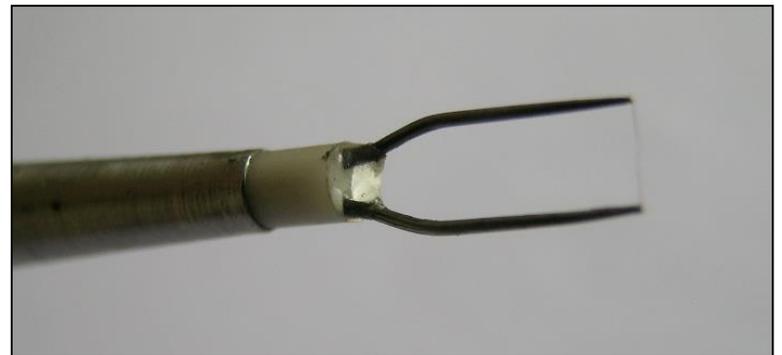
up to 60 kHz



*Basic research tool  
in turbulence*

TODAY'S PRESENTATION:

*Investigation of the dynamic  
response of a CTHWA  
system*



# Why CTHWA?

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Hot-Wire Anemometry  
(CTHWA)**

High spatial resolution:

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High frequency response:

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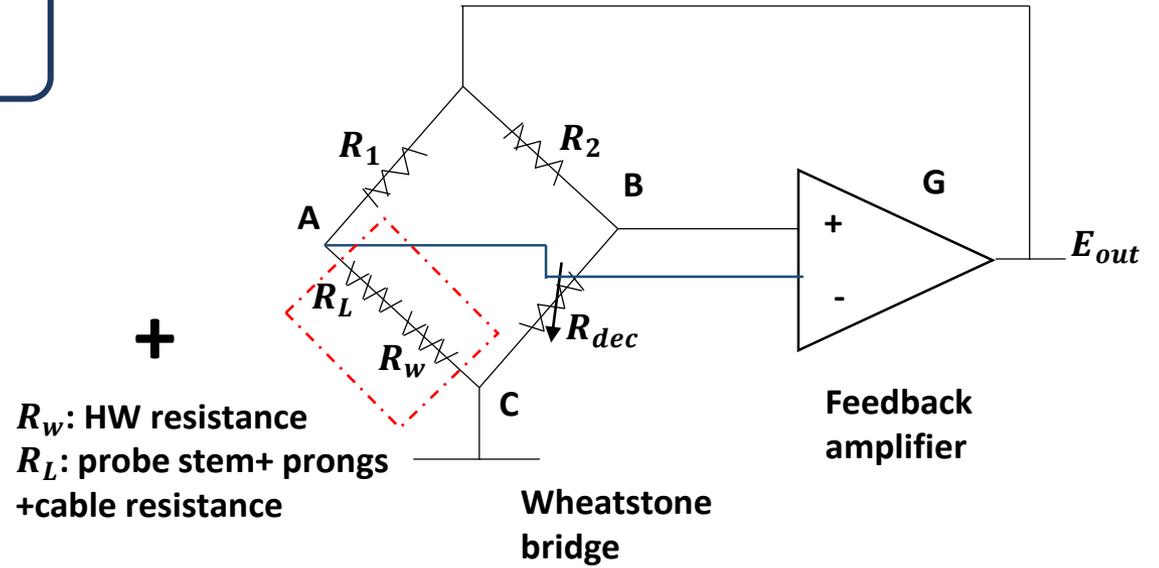
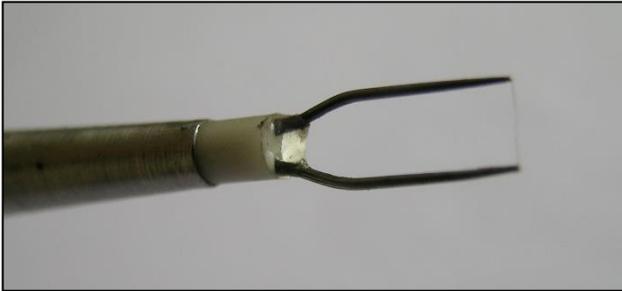
TODAY'S PRESENTATION:

*Investigation of the dynamic  
response of a CTHWA  
system*

*HWA is an established  
technique. What is left to  
investigate?*

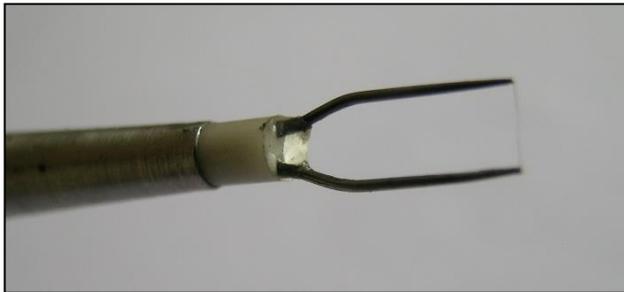
# CTHWA

CTHWA: probe + electronics



# Square wave test

CTHWA: probe + electronics

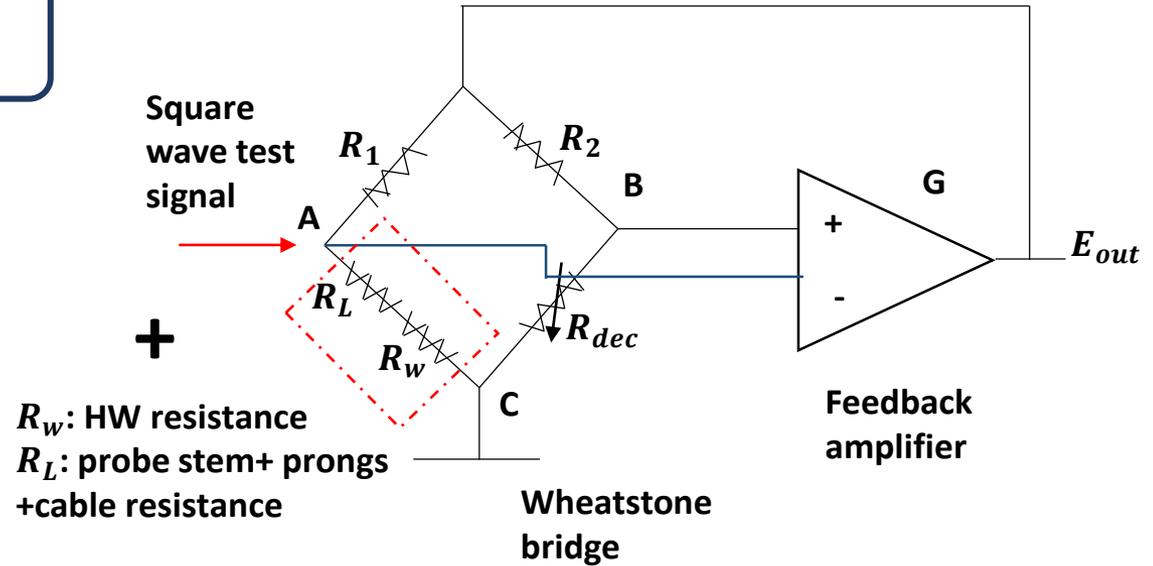


Common method for dynamic response optimization:

Square wave voltage perturbation



**Velocity impulse perturbation**

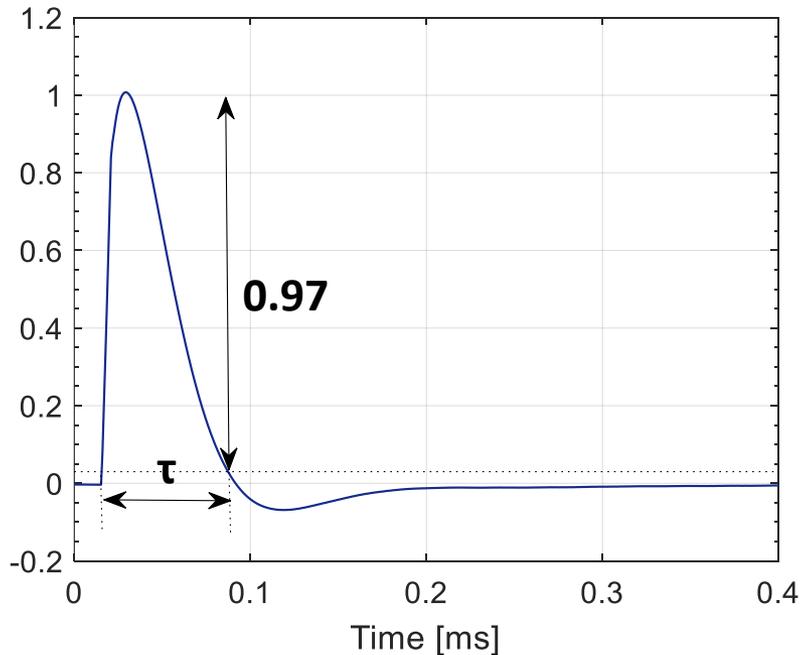


“square wave test”



# CTHWA typical use

Optimized response to square wave

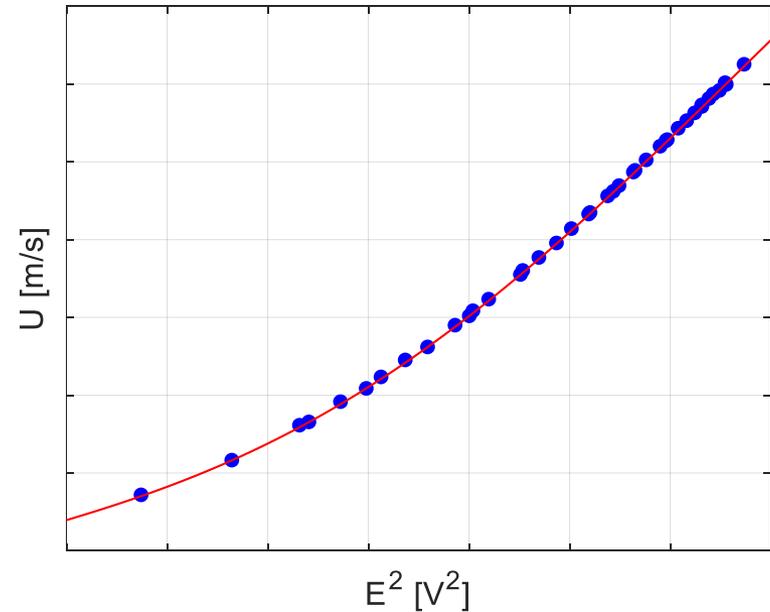


$$f_{cut} = \frac{1}{1.3\tau} : -3 \text{ dB attenuation}$$

Response assumed flat up to  $f_{cut}$

Static calibration used

Static calibration



$$U = f(E^2)$$

→ Dynamic response effects neglected!

# In this work:

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GOAL:

*Highlight often neglected effects of the dynamic behavior of CTHWA on the measurement of turbulence*

USING:

**Numerical model**

**+**

**Experimental square  
wave test**

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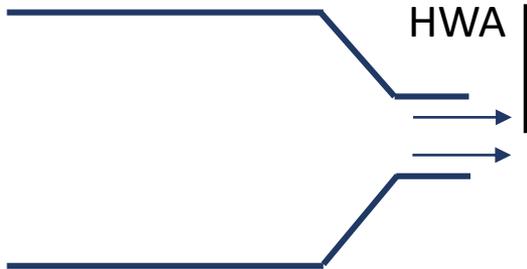
**Numerical model**

**+**

**Experimental square  
wave test**

- ❖ Thermal transient effects due to heat conduction to the wire supports
- ❖ Non-linear effects important for large fluctuations
- ❖ Is the square wave test equivalent to the response to a velocity perturbation?

# Experimental method



- HW probe placed in the flow (Response depends on the flow conditions)

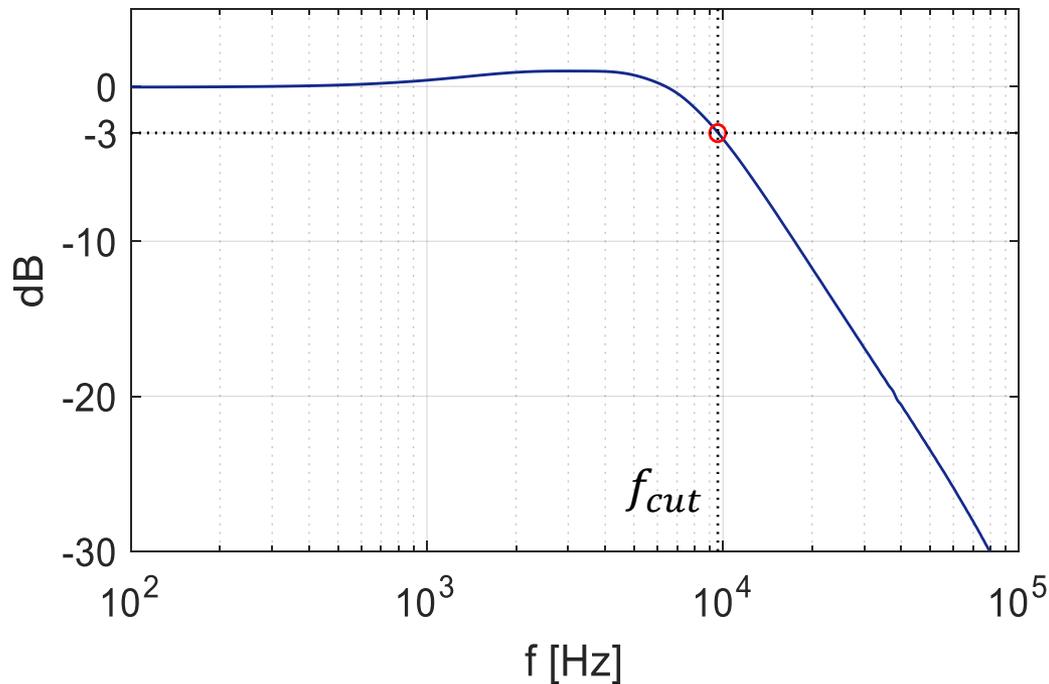
- Using the embedded square wave voltage generator of the Dantec Streamline system, acquire the signal with  $f_s = 1.25 \text{ MHz}$



- Phase averaging to eliminate effect of flow fluctuations and obtain a clean signal

# Experimental method

- Compute Fourier transform of averaged response
- System is a “black-box”, unknown amplitude of input voltage



- To compute transfer function:  
Non-dimensionalization with  
amplitude at low frequency, where  
amplitude can assumed to be 1

***Amplitude transfer function***

# Numerical model

Proposed by Freymuth (1977) & used by Weiss et al. (2013):

## 1. Wheatstone bridge equation:

$$\delta = \frac{R_1(R^* - R_w)}{(R_1 + r_L + R^*)(R_1 + r_L + R_w)} E + M_B \frac{dE}{dt} + \frac{R_1(r_L + R_w)}{(R_1 + r_L + R_w)} \frac{E_t}{R_t}$$

Term only present  
for the square wave  
test

## 2. Amplifier equation:

$$M'' \frac{d^2 E}{dt^2} + M' \frac{dE}{dt} + E = G\delta + E_B$$

## 3. Wire equation:

$$m_w c_w \frac{\partial T_w}{\partial t} = \frac{E^2 R_w}{(R_1 + r_L + R_w)^2} - Nu \pi l_w k_f (T_w - \eta T_0) - k_w A_c \frac{\partial^2 T_w}{\partial x^2}$$

heat  
conduction  
term

Convection losses term for  
non-dimensional calibration

$$Nu = f(Re)$$

# Numerical model

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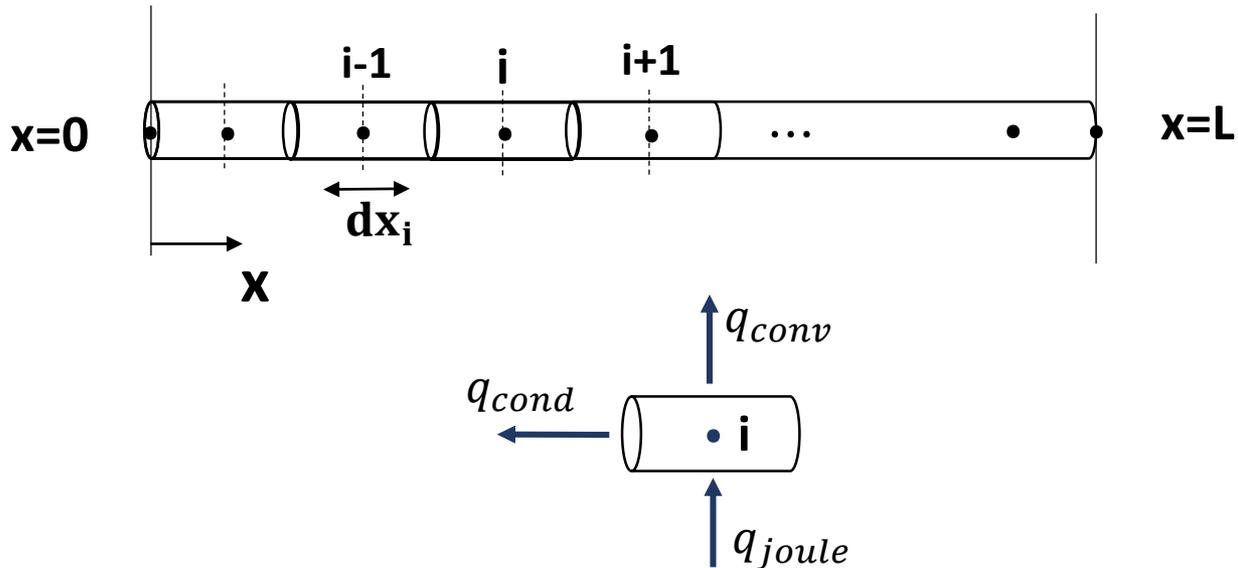
$$m_w c_w \frac{\partial T_w}{\partial t} = \frac{E^2 R_w}{(R_1 + r_L + R_w)^2} - Nu\pi l_w k_f (T_w - \eta T_0) - k_w A_c \frac{\partial^2 T_w}{\partial x^2}$$



*System of 2 ODEs and 1 PDE*

# Numerical solution

- ❖ The wire is discretized in  $n-1$  elements and  $n$  nodes

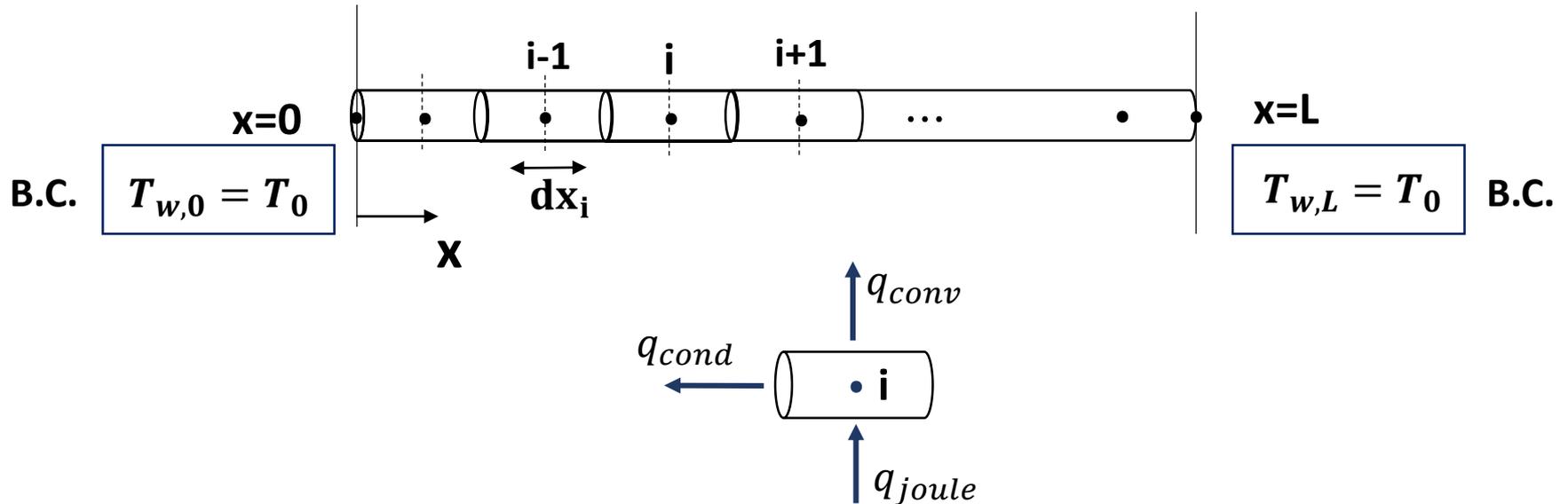


- ❖ The spatial derivative is discretized and the wire equation is written for each node:

$$m_{w,i}c_{w,i} \frac{\partial T_{w,i}}{\partial t} = \frac{E^2 R_{w,i}}{(R_1 + r_L + R_{w,tot})^2} - Nu_i \pi l_i k_f (T_{w,i} - \eta T_0) - k_w A_{c,i} \frac{T_{w,i+1} - 2T_{w,i} + T_{w,i-1}}{dx_i}$$

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**System of  $n+2$  ODEs**

**Solve with Runge-Kutta method**

# Numerical solution

Wire equation:

$$m_{w,i}c_{w,i} \frac{\partial T_{w,i}}{\partial t} = \frac{E^2 R_{w,i}}{(R_1 + r_L + R_w)^2} - Nu_i \pi l_i k_f (T_{w,i} - \eta T_0) - k_w A_{c,i} \frac{T_{w,i+1} - 2T_{w,i} + T_{w,i-1}}{dx_i}$$

└ Temperature profile along the wire at each time instant

$T_w$  spatial average and  
corresponding  $R_w$

$$T_w = \frac{1}{L} \int_0^L T_w(x) dx$$

$$R_w = R_{ref} (1 + a_w (T_w - T_{ref}))$$

Input to

Wheatstone bridge equation:

$$\delta = \frac{R_1 (R^* - R_w)}{(R_1 + r_L + R^*) (R_1 + r_L + R_w)} E + M_B \frac{dE}{dt} + \frac{R_1 (r_L + R_w)}{(R_1 + r_L + R_w) R_t} \frac{E_t}{R_t}$$

# Circuit parameters' estimation

Commercial system used, certain circuit parameters are not know:

$$G, M', M'', E_b, M_B$$

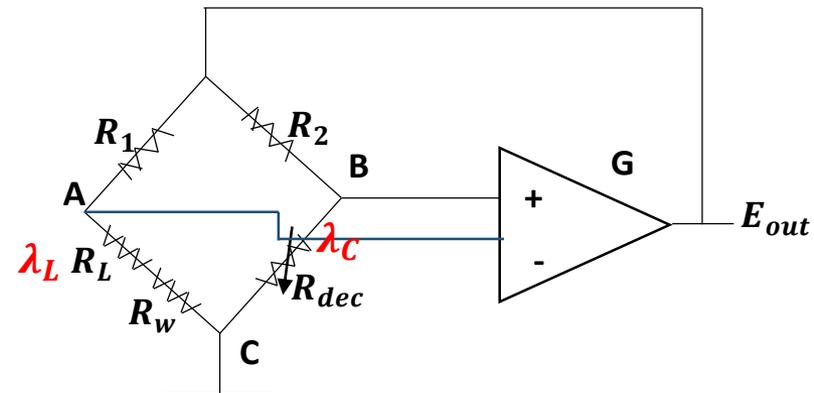
- $E_b$ , offset voltage of the amplifier. No adjustment in our system. Increases the damping of the system, a constant high value is selected following Perry (1972).

$$E_b = 5 V$$

- $M_B$ , bridge time constant takes into account high frequency components. It is adjusted by varying an inductance  $\lambda_L$  of a set of coils to compensate for the inductance of the cable  $\lambda_C$  (Freytmuth 1977),

$$M_B = \frac{\lambda_L/R_2 - \lambda_C/R_1}{(n + 1)^2} = 10^{-10}$$

- G, amplifier gain. Adjusted during square wave test.
- $M', M''$  time constants of the amplifier. Adjusted during square wave



# Comparison with experiments

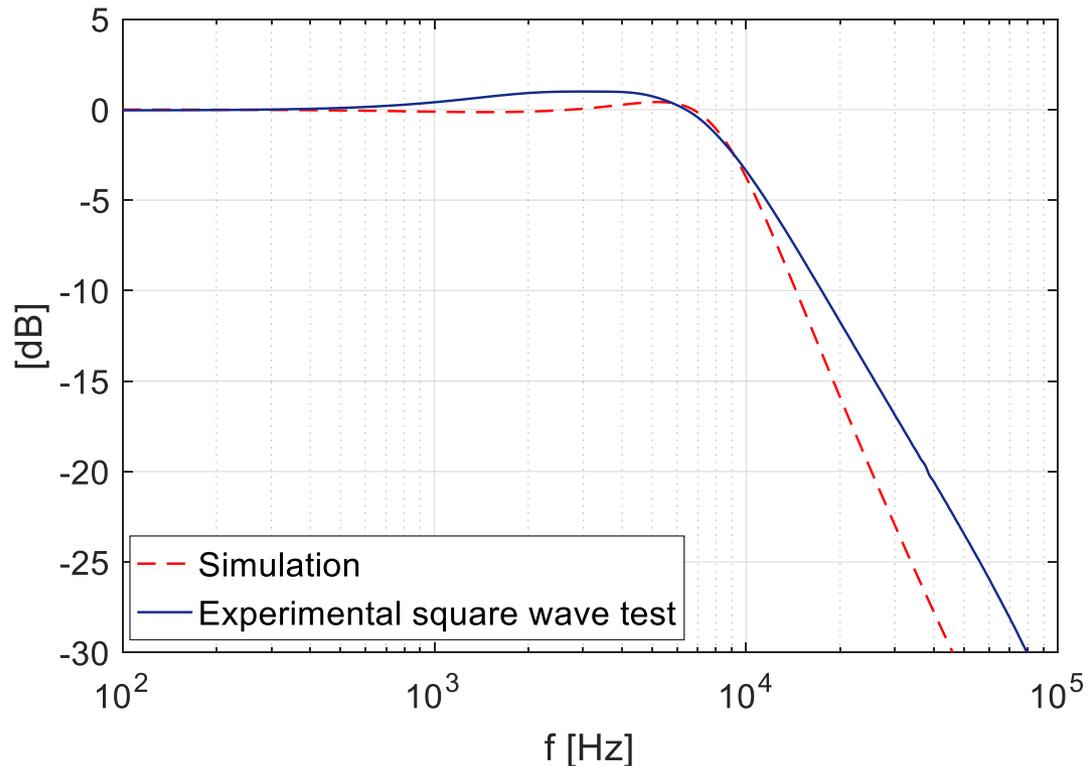
Comparison of the model with experimental square wave test

Tungsten wire  
 $d_w = 9 \mu m$   
 $l_w = 1 mm$   
 $T_w = 455 K$   
 $M=0.25$

$G = 230$   
 $M' = 1.6 \cdot 10^{-5}$   
 $M'' = 10^{-11}$



To predict the same  $f_{cut}$



- Steeper attenuation at high frequencies
- Different behavior at low frequencies

**Further investigation required!**

# In this work:

GOAL:

*Highlight often neglected effects of the dynamic behavior of CTHWA on the measurement of turbulence*

USING:

**Numerical model**

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**Experimental square  
wave test**

- ❖ Thermal transient effects due to heat conduction to the wire supports
- ❖ Non-linear effects important for large fluctuations
- ❖ Is the square wave test equivalent to the response to a velocity perturbation?

# Velocity vs voltage perturbation

<i>Voltage perturbation</i> <i>“square wave test”</i>	<ul style="list-style-type: none"><li>❖ Electronic testing</li><li>❖ Common method to test dynamic response</li></ul>
<i>Velocity (Reynolds) perturbation</i>	<ul style="list-style-type: none"><li>❖ Direct testing</li><li>❖ Real case</li><li>❖ Difficult to perform</li></ul>

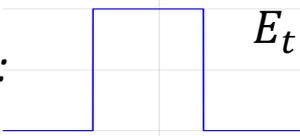
*The square wave test should be always used to adjust the response and avoid a self-oscillating system*

*BUT can it be used as a reliable estimation of the system’s response?*



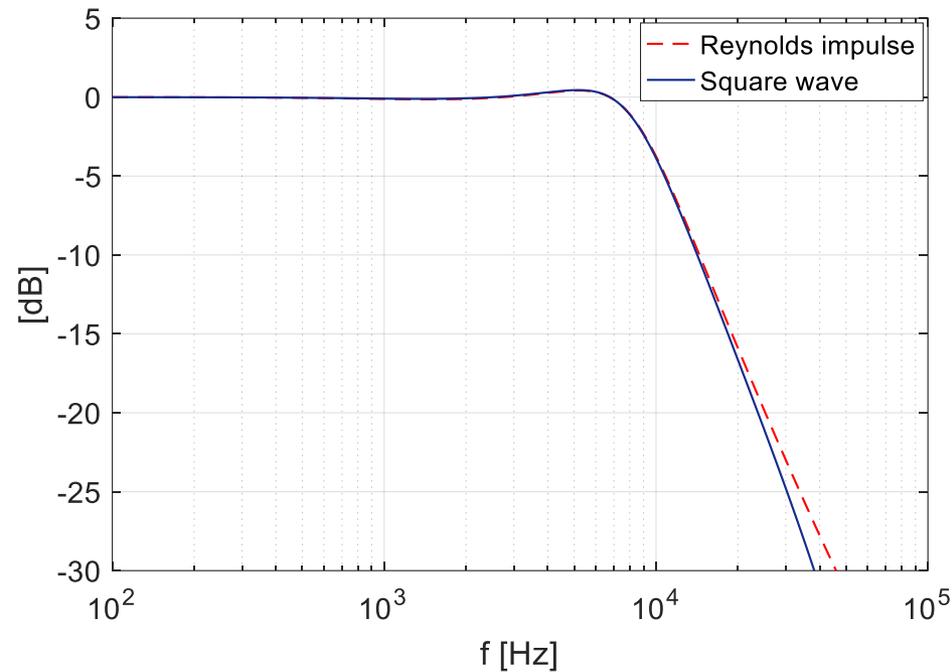
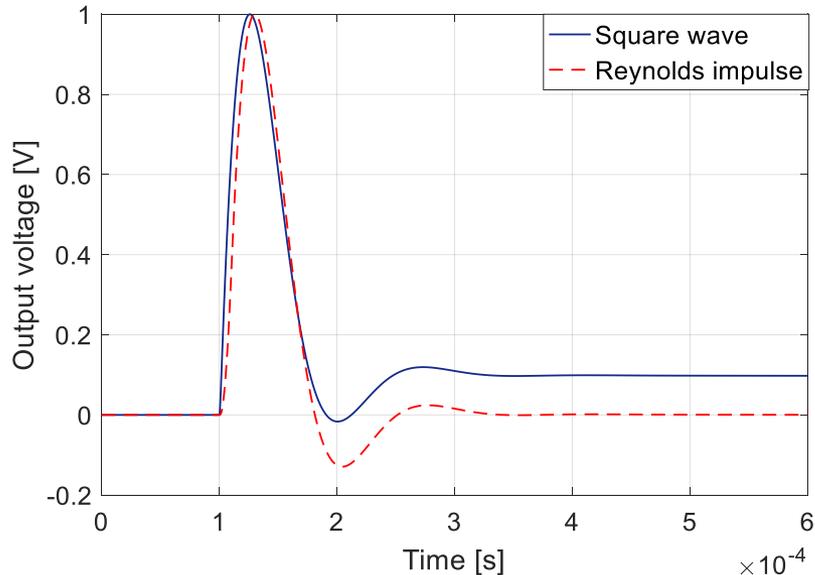
*Disagreement in literature*

Use the model to simulate both cases:

- Case1, Inputs:   $E_t$   $Re = const$
- Case2, Inputs:   $Re$   $E_t = 0$

# Velocity vs voltage perturbation

**Compare response to square wave voltage and response to Reynolds impulse**

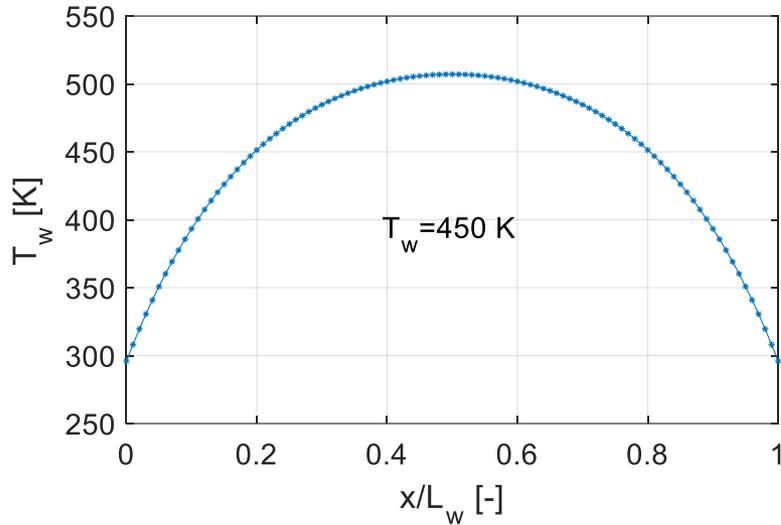


Only difference at high frequencies

Square wave seems to simulate adequately Reynolds impulse

Transfer function could be used to correct amplitude

# Thermal transient effects



Low frequency attenuation due to heat conduction to the wire supports from  $f_l \sim 150$  Hz

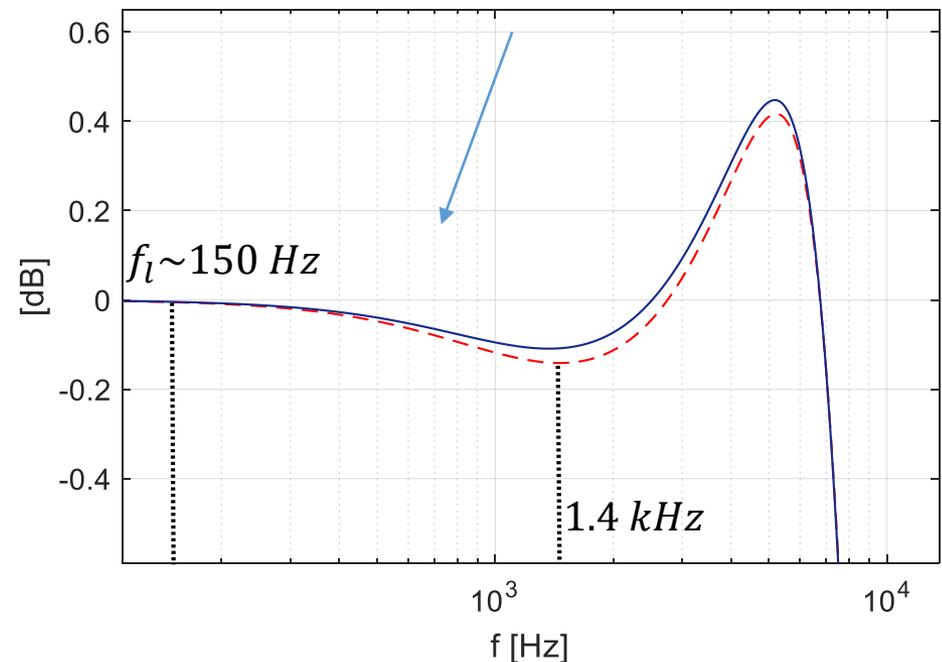
From  $f > 1.4$  kHz amplification due to system dynamics, attenuation not completed

Temperature profile along the wire

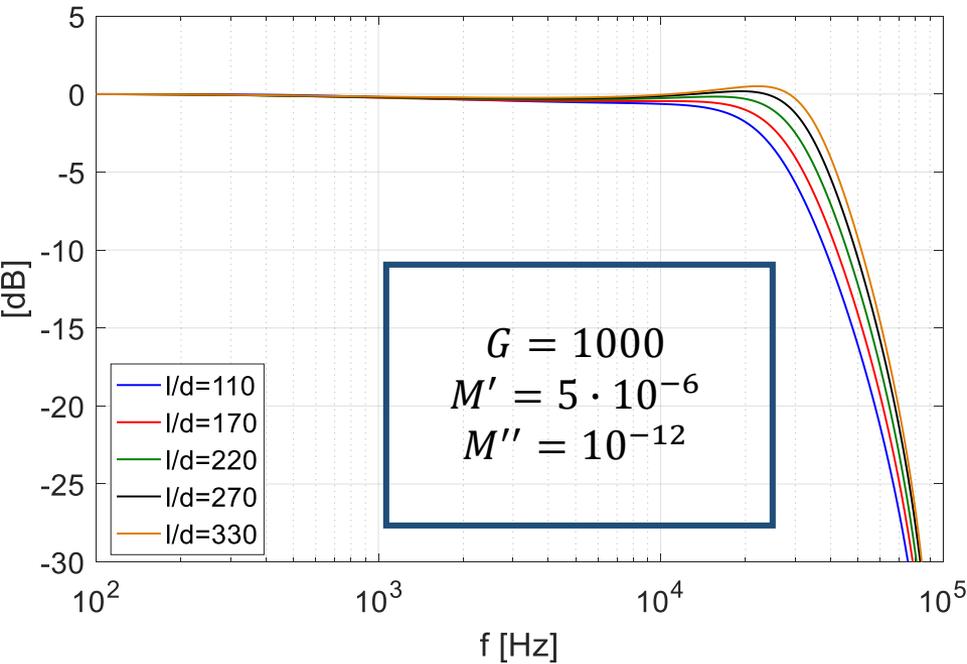
$$T_w = 450 \text{ K}$$

$$T_{w,exp} = 455 \text{ K}$$

**Square wave response also features attenuation**



# Thermal transient effects



High  $l/d$



convection > conduction

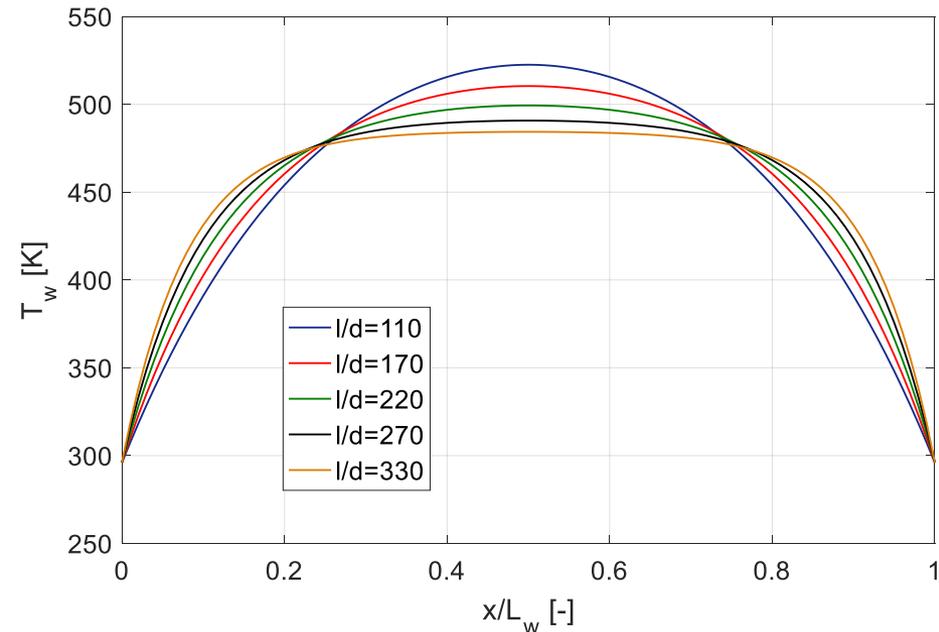
Flatter  $T_w$  distribution

Adjust amplifier parameters to move cut-off to higher frequencies

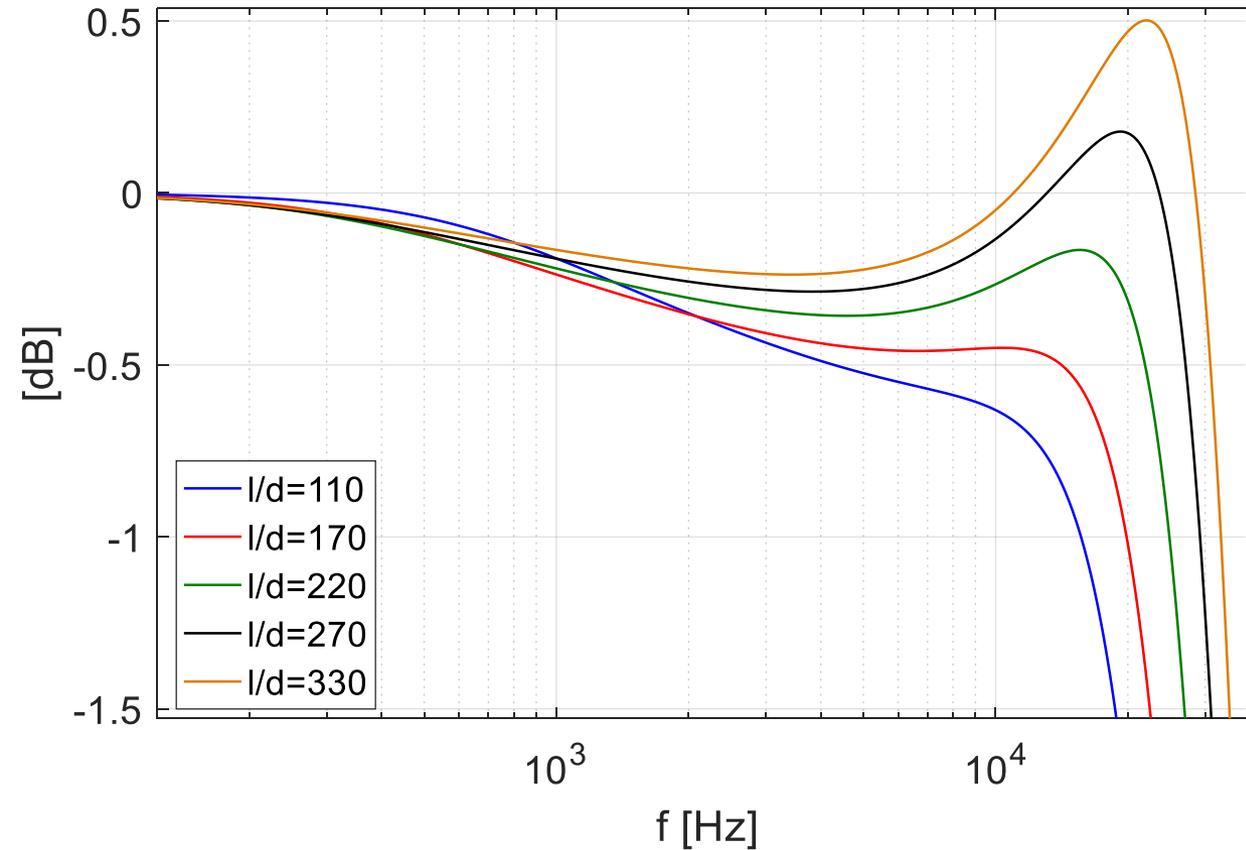


Focus on attenuation

$l/d$  ratio effect



# Thermal transient effects



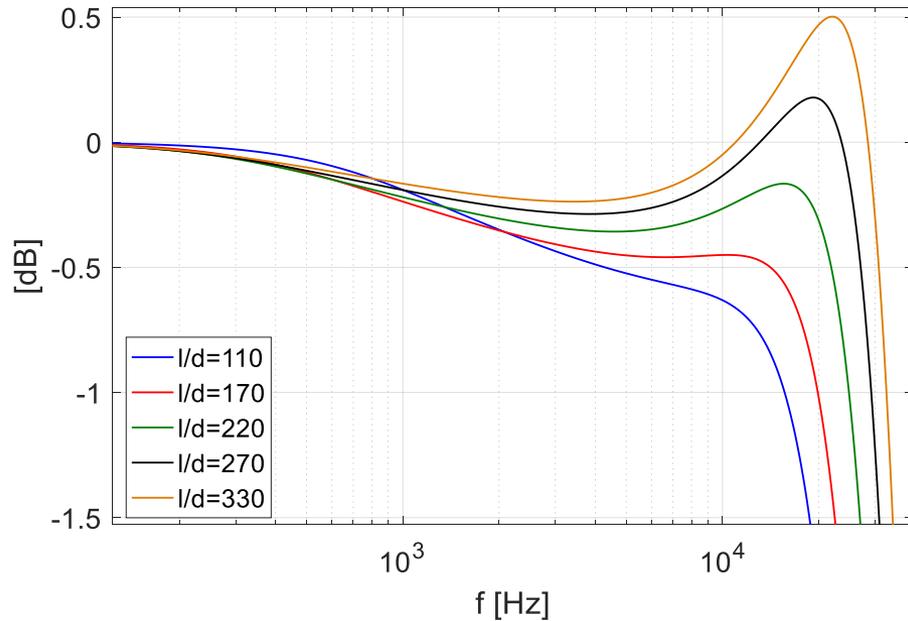
High  $l/d$   
↓  
Final attenuation value decreases

High  $l/d$  should be used for less attenuation  
Small  $l$  should be used for spatial resolution  
Min  $d$  restricted by mechanical strength



Trade-off  
Choice depends on application

# Thermal transient effects

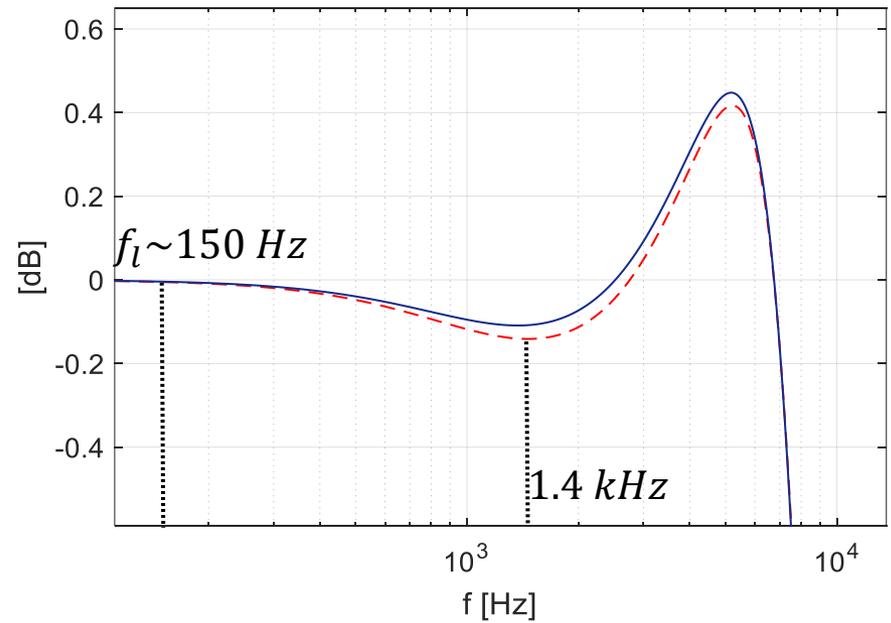


Attenuation important for a wide range of frequencies even for  $l/d=330$

Correction should be applied

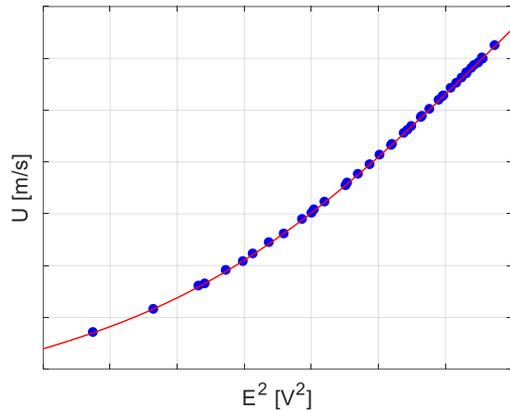
Attenuation also present at square wave test response, negligible difference

**Square wave transfer function could be used for correction**



# Non-linearity

The response of CTHWA is non-linear



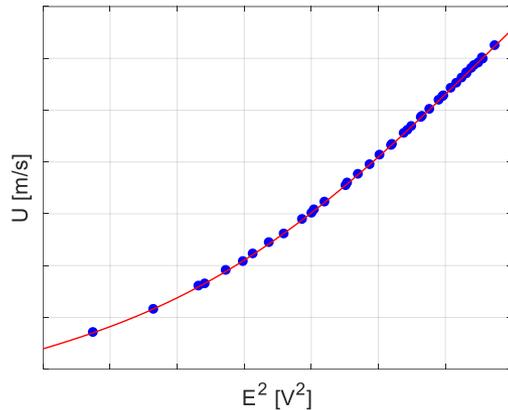
Non-linear static response  
heat transfer law

+

Non-linear dynamic response  
Bridge and wire equations of the  
dynamic model

# Non-linearity

The response of CTHWA is non-linear



Non-linear static response  
heat transfer law

Corrected with calibration

+

Non-linear dynamic response  
Bridge and wire equations of the  
dynamic model

Usually neglected

Valid for small fluctuations

Errors for large fluctuations



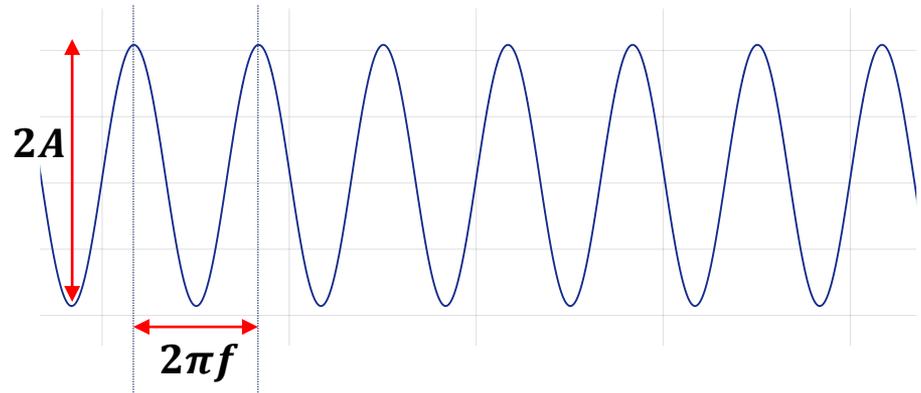
***Turbomachinery flows!***

*Errors mainly affect odd turbulence moments,  
e.g. skewness*

# Non-linearity

Reynolds input to the model:

$Re_{in}$



Static calibration

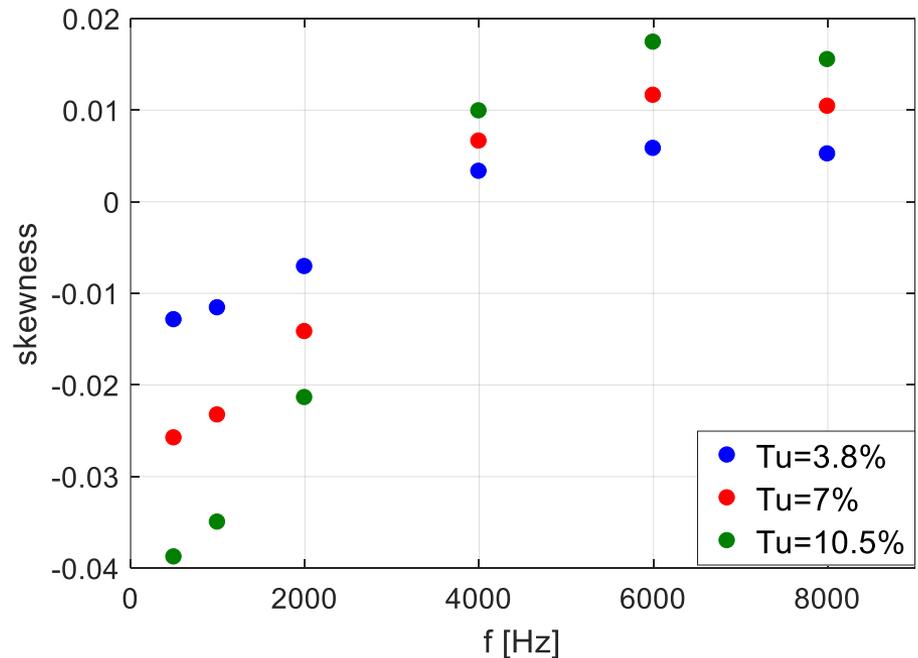
Output voltage  $\longrightarrow$  Output Reynolds  $Re_{out}$

Skewness of  $Re_{out}$

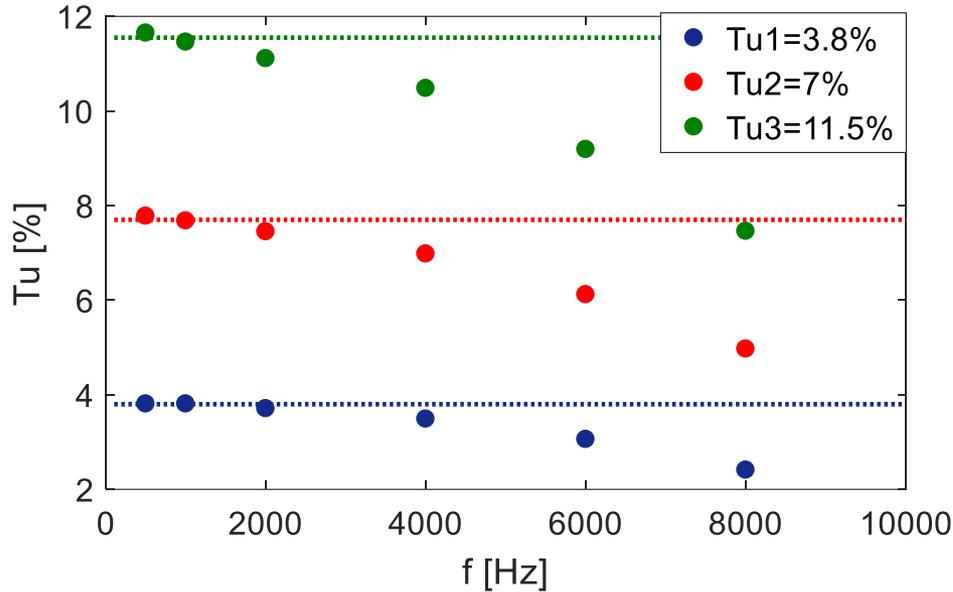


Increasing with increasing amplitude

Results agree with Weiss et al. (2013)



# Non-linearity



For increasing frequency:

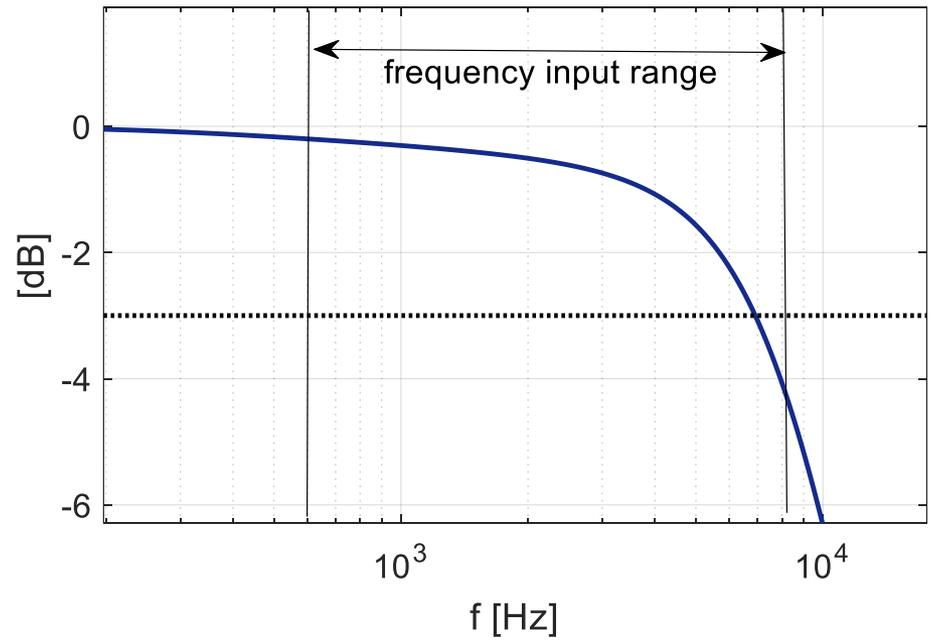
$$T_{u,out} < T_{u,in}$$

Range of input frequencies  
affected by attenuation

Heat conduction attenuation  
+system damping

Significant attenuation

Correction should be applied!



# Conclusions

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- ❖ Identification of possible sources of errors in turbulence measurements due to the dynamic response of CTHWA :
  - Attenuation due to heat conduction
  - Amplification or damping due to system dynamics
  - Non-linearity errors
  
- ❖ For small fluctuations, the first two could be corrected by applying a transfer function to the measured spectrum. According to this model, the transfer function obtained with the square wave test could be used but further validation is required.
  
- ❖ For large fluctuations the effect of non-linearity can have a significant effect on the skewness. It can not be corrected by a transfer function. Correction method existing for Constant-Voltage-Anemometry (Berson et al. 2009) but not for CTHWA.

# Future work

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- ❖ Further work on the validation of the dynamic model:
  - Use a VKI anemometer instead of a Dantec system to better estimate the circuit parameters
  - Consider direct testing (eg by laser heating) in addition to the electronic testing
- ❖ Further work on the possibility of corrections.
- ❖ Use of the model for the design of HW probes with optimized response
- ❖ Investigate spatial resolution issues

# References

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- ❖ P. Freymuth, (1977), Further Investigation of the Nonlinear Theory for Constant-Temperature Hot-Wire Anemometers, *Journal of Physics E: Scientific Instruments* 10.
- ❖ J. Weiss, A. Berson, G. Comte-Bellot, (2013) Investigation of Non- Linear Effects in Constant Temperature Anemometers, *Measurement Science and Technology* 24.
- ❖ A. Berson, P. Blanc-Benon, G. Comte-Bellot, (2009), A Strategy to Eliminate All Nonlinear Effects in Constant-Voltage Hot-Wire Anemometry, *Review of Scientific Instruments* 80.
- ❖ A. E. Perry, G. L. Morisson, (1971) A Study of the Constant- Temperature Hot-Wire Anemometer, *Journal of Fluid Mechanics* 47 (3).

Thank you for your attention!